

# Introduction to Incoherent Scatter Radar – Part 2: Scatter

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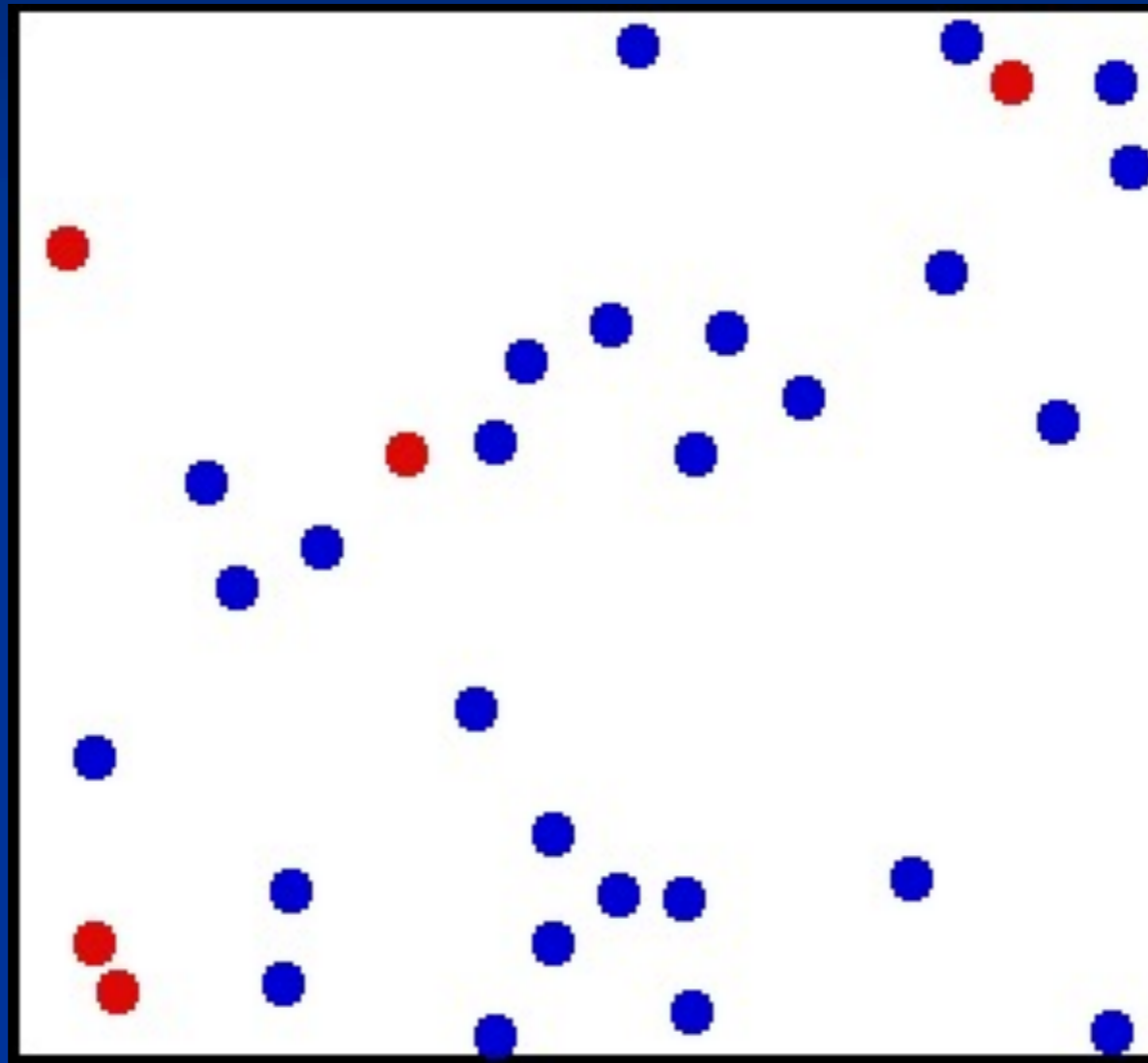
And my advisor: William E. Gordon

# Incoherent Scatter Radar

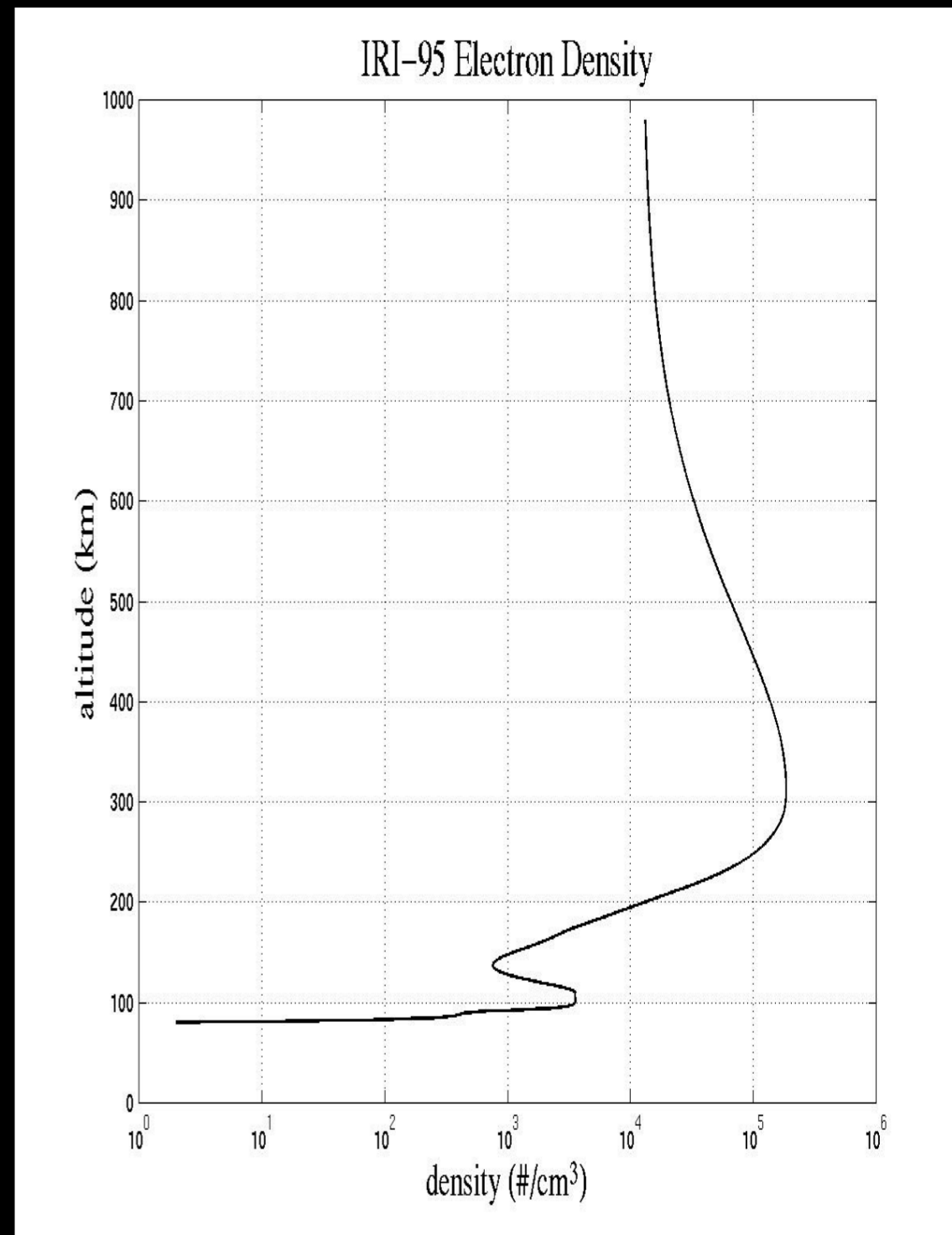
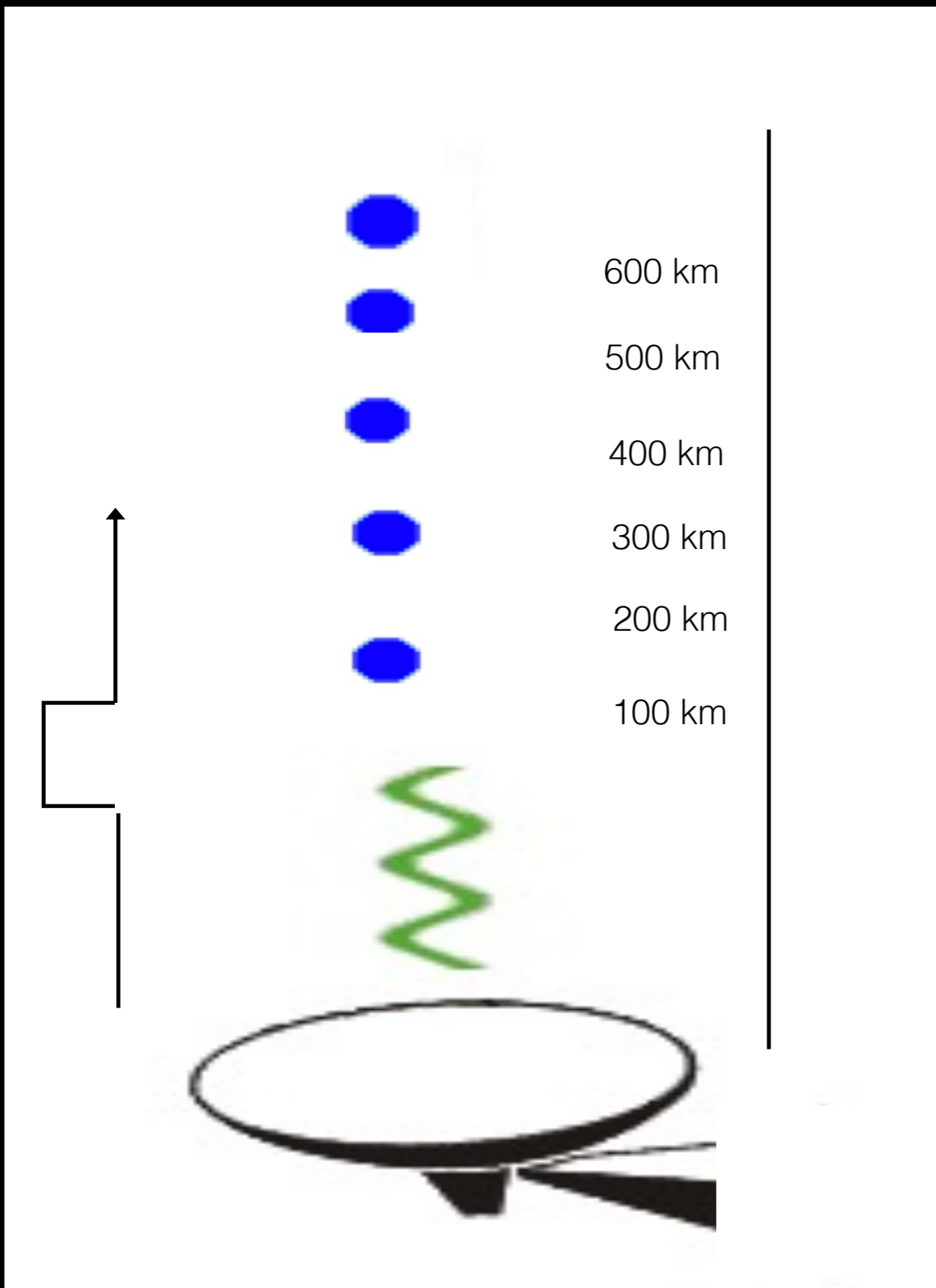
- Radar
- Scatter
- Incoherent

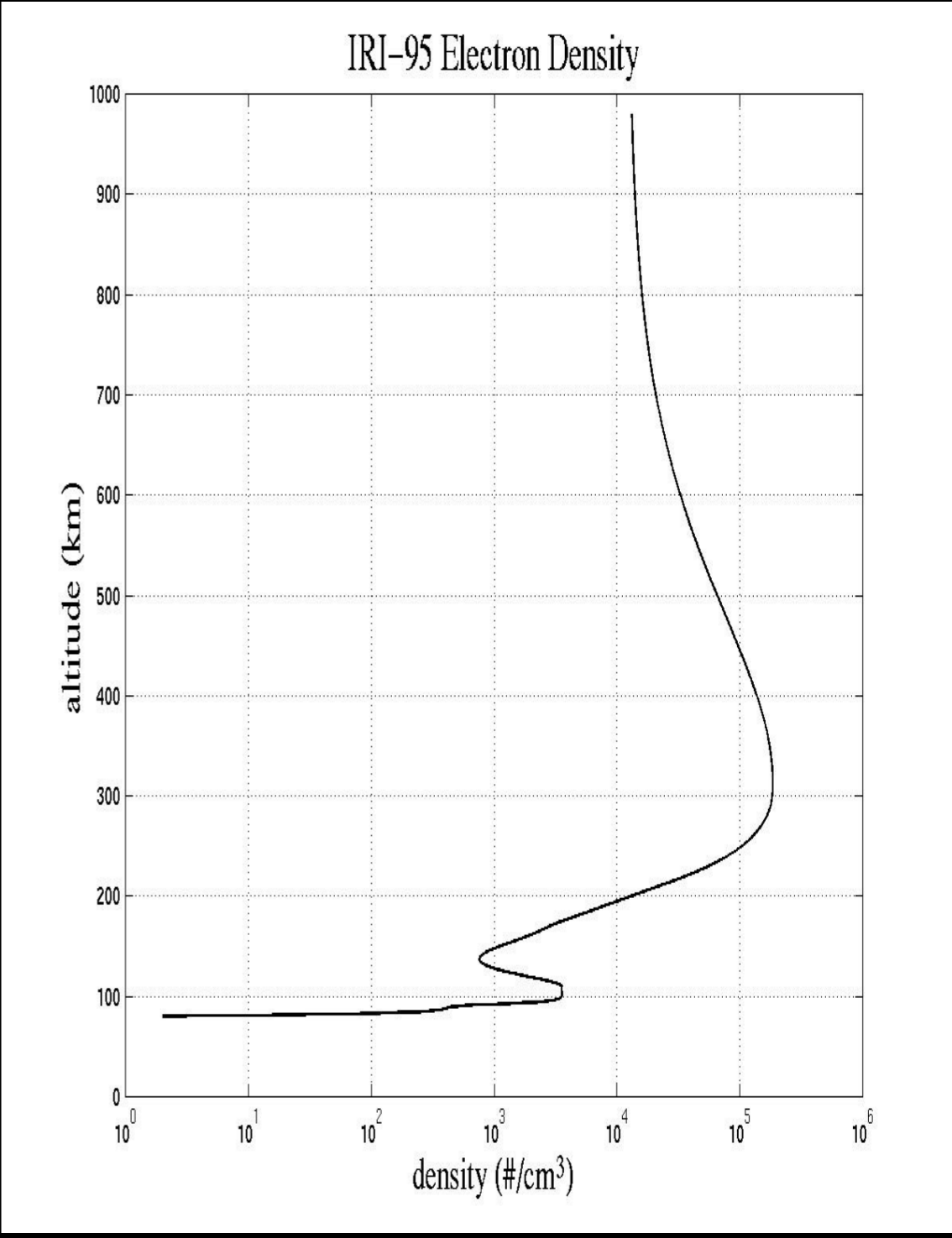
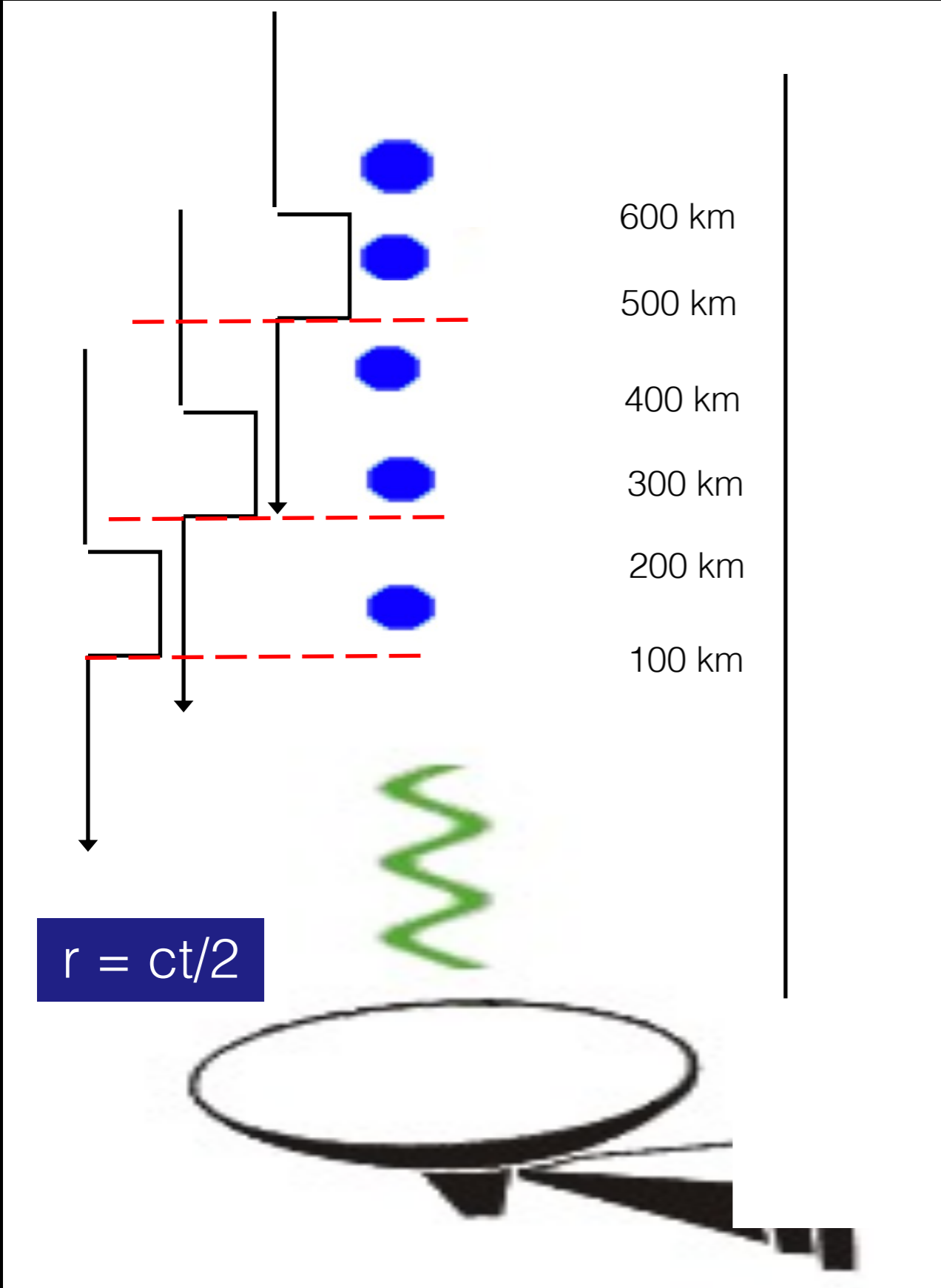


# Thermal fluctuating electrons



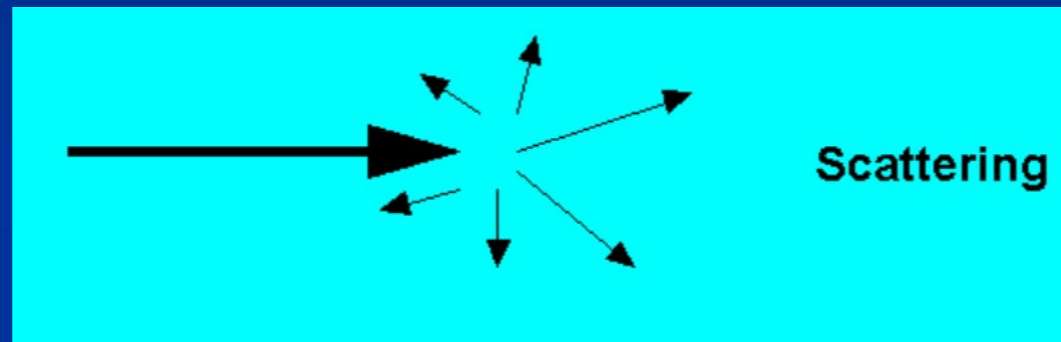
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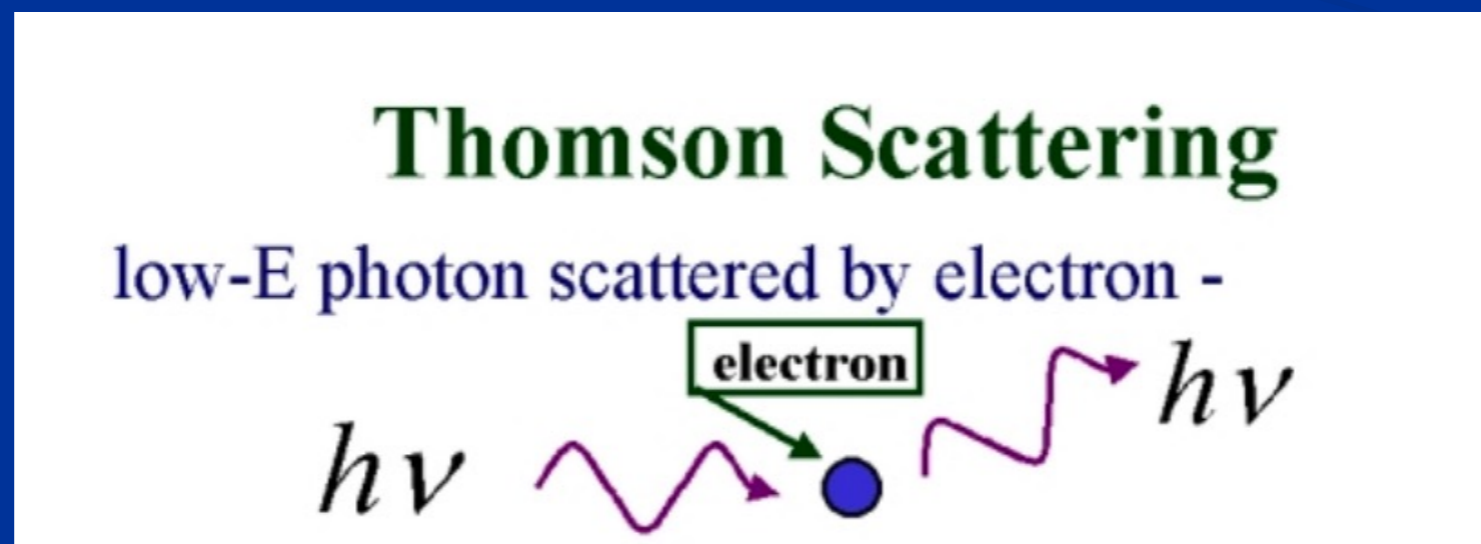


# Thomson scattering

- Thomson scattering is the elastic scattering of electromagnetic radiation by a free charged particle, as described by classical electromagnetism.

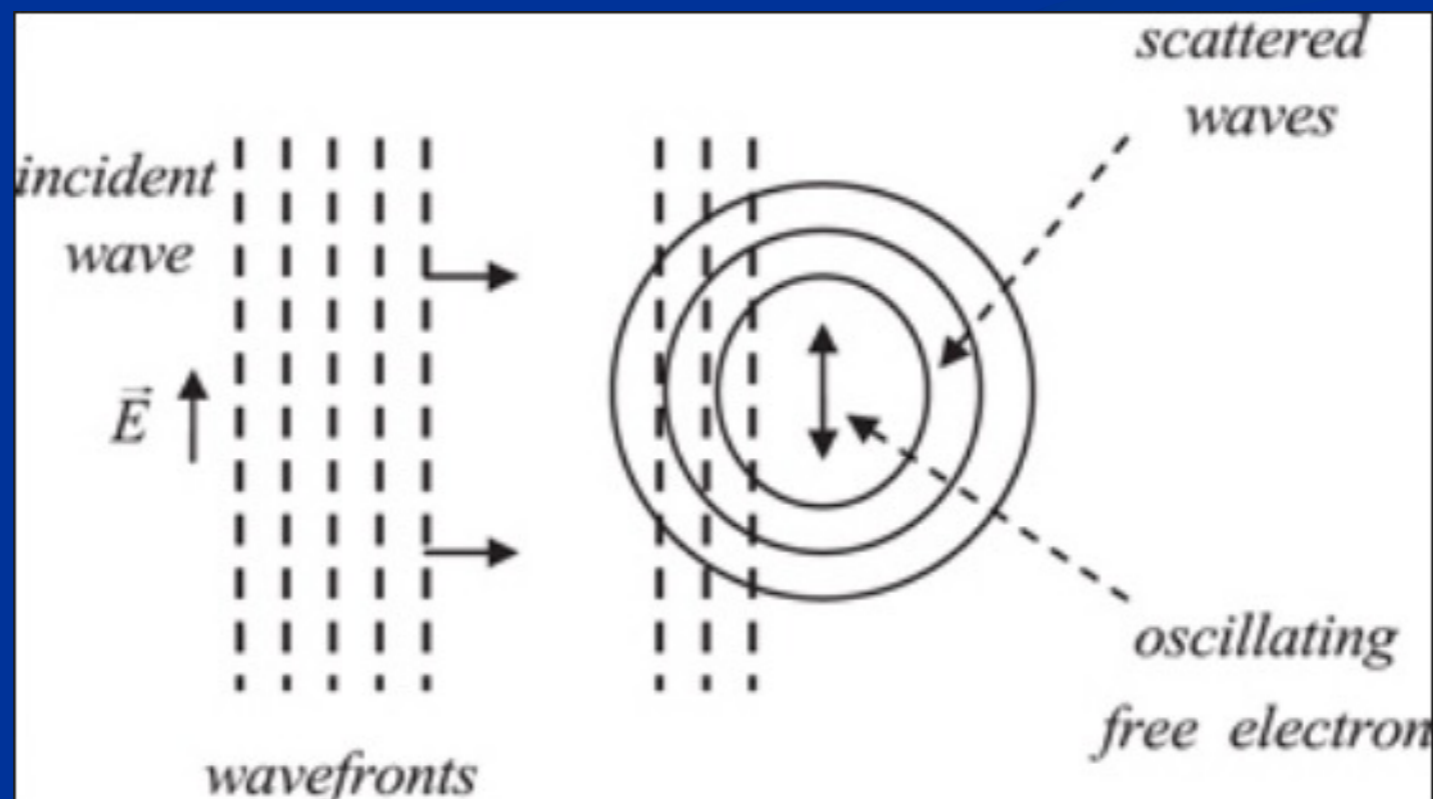


- In the low-energy limit, the electric field of the incident wave (radar wave) accelerates the charged particle, causing it, in turn, to emit radiation at the same frequency as the incident wave, and thus the wave is scattered.



# Thomson scattering (con.)

- As long as the motion of the particle is non-relativistic (i.e. its speed is much less than the speed of light), the main cause of the acceleration of the particle will be due to the electric field component of the incident wave, and the magnetic field can be neglected. The particle will move in the direction of the oscillating electric field, resulting in electromagnetic dipole radiation





# Thomson Scattering

$$E_x = E_0 e^{j(\omega t - kx)}$$

$$\vec{F} = q(\vec{E} + \vec{v} \times \vec{B})$$

$$v_x = -j \frac{q_e E_0}{m_e \omega} e^{j\omega t}$$

$$E_\phi = \frac{\mu_0 q_e^2}{4\pi m_e} \frac{\sin \phi}{r} e^{-jkr} E_0$$

$$\sigma_e = 4\pi \left( \frac{\mu_0 q_e^2}{4\pi m_e} \right)^2 \sin^2 \phi = 4\pi r_e^2 \sin^2 \phi$$
$$\approx 10^{-28} \sin^2 \phi \quad (\text{m}^2)$$



# Doppler Radar - frequency domain

