

# Introduction to heating experiments

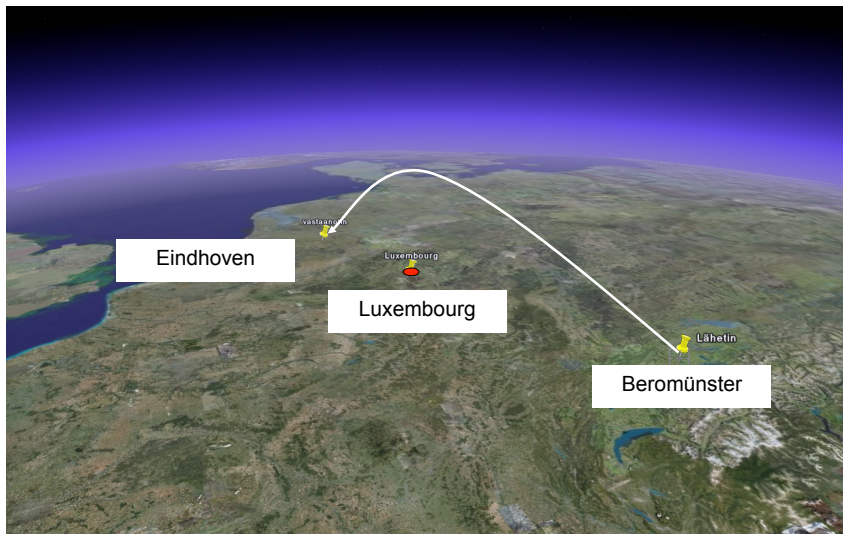
Antti Kero

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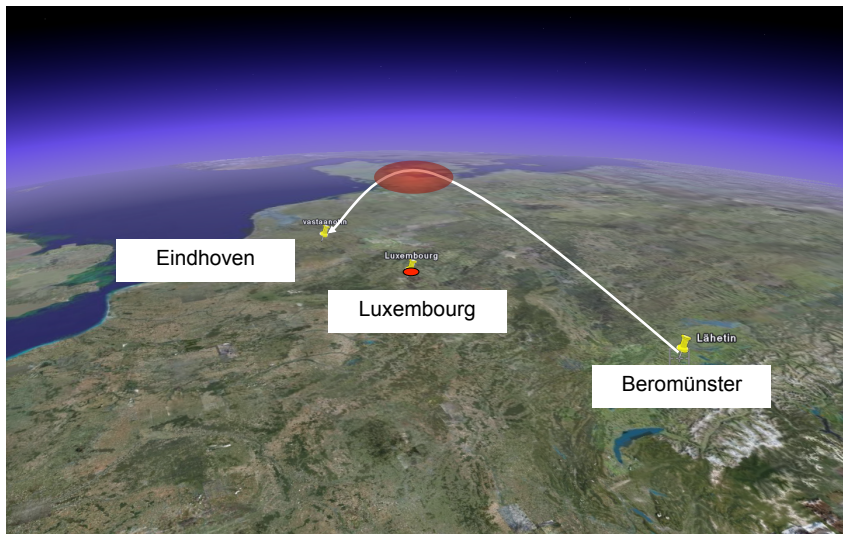
[antti.kero@sgo.fi](mailto:antti.kero@sgo.fi)

ISR School, Puerto Rico, 2014

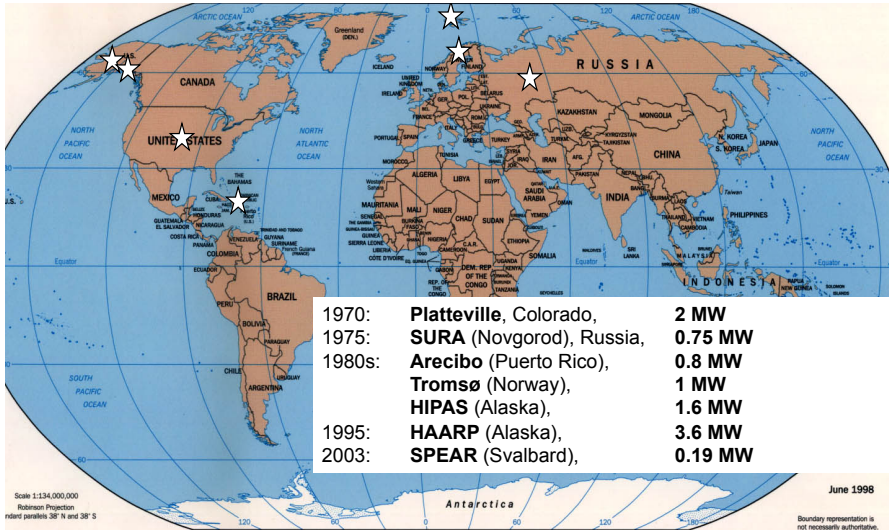
# Early history: Luxembourg effect 1933



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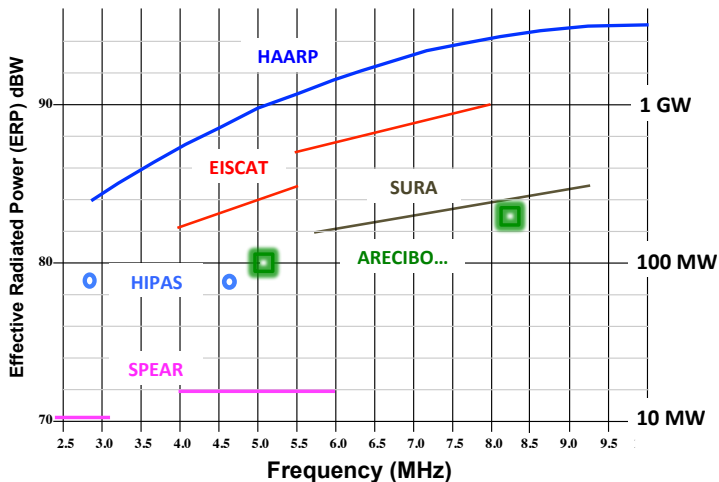


# Heating facilities: POWER to the people!

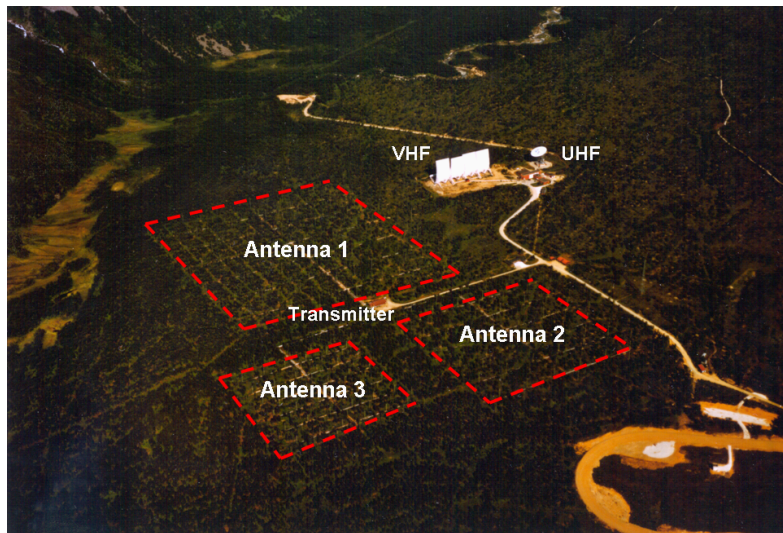




# Heating facilities: ERP to the people!



# Heating facilities: EISCAT, Norway



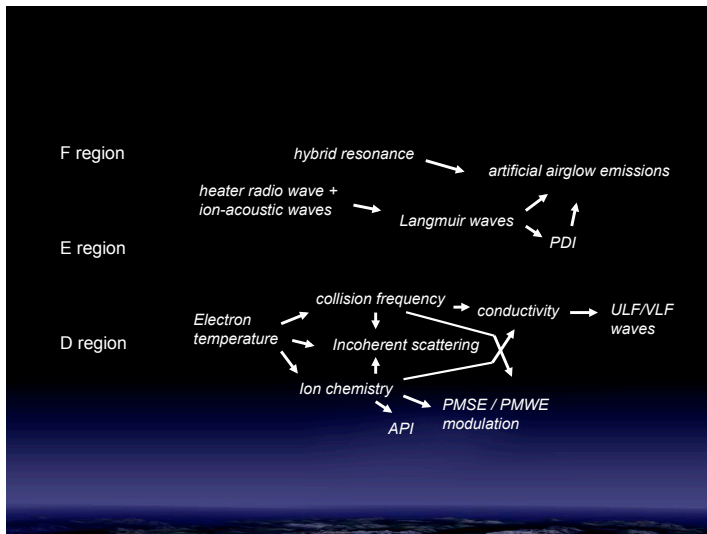
# Heating facilities: Arecibo, Puerto Rico



# Heating facilities: HAARP, Alaska



# Some science applications



## Heating effect in collisional plasma: Appleton equation

Refractive index  $n$  of the plasma for the radio wave is given by the Appleton equation

$$n^2 = 1 - \frac{X}{1 - iZ - \frac{(Y \sin \alpha)^2}{2(1-X-iZ)} \pm \sqrt{\frac{(Y \sin \alpha)^4}{4(1-X-iZ)^2} + (Y \cos \alpha)^2}},$$

where the normalised frequencies are

$$X = \frac{\omega_{pe}^2}{\omega^2} = \frac{N_e e^2}{\epsilon_0 m_e \omega^2}, \quad Y = \frac{\omega_{ge}}{\omega} = \frac{eB}{m_e \omega} \text{ and } Z = \frac{\nu_{en}}{\omega}.$$

## Heating effect in collisional plasma: energy absorption

When the complex refractive index  $n = \Re(n) + i\Im(n)$ , given by the Appleton equation, is applied to the plane wave equation

$$E(r, t) = E_0 \exp[i\omega (t - nr/c)]$$

we get a decaying wave in a case of  $\Im(n) < 0$ :

$$E(r, t) = E_0 \exp[i\omega (t - \Re(n)r/c)] \exp(\omega\Im(n)r/c).$$

## Heating effect in collisional plasma: energy absorption

Since the intensity of the wave  $I \propto E^2$ ,

$$I(r) = \frac{ERP}{4\pi r^2} \exp\left(\frac{2\omega}{c} \int_0^r \Im(n) dr\right),$$

and the absorbed energy per time unit and per volume is

$$Q = -\frac{dl_{abs}}{dr} = -2\omega \Im(n) I / c.$$

This is the energy gain from the wave to the plasma due to collisions between electrons (accelerated by the wave) and neutrals.



# Heating effect in collisional plasma: electron energy budget

In the ideal gas, the mean electron energy is

$$E = \frac{3}{2} k_B T_e.$$

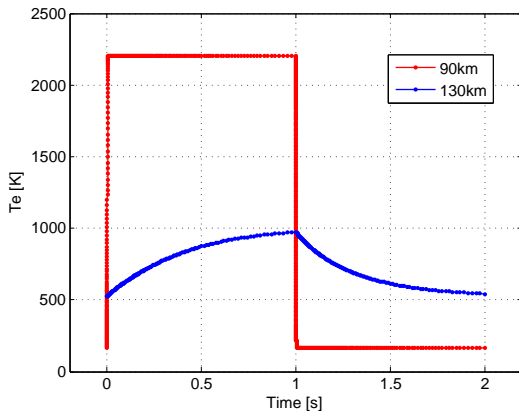
By differentiating this with respect to volume and time, we get

$$\frac{dT_e}{dt} = \frac{2}{3k_B N_e} (Q - L) = \frac{2}{3k_B N_e} \left( \frac{-2\omega \Im(n) I}{c} - L \right).$$

Here  $L = \sum L_X ([X], N_e, T_n, T_e)$  denotes the sum of electron energy loss processes by excitations of  $O_2$ ,  $N_2$  and  $O$  (Stubbe ja Varnum, 1972).

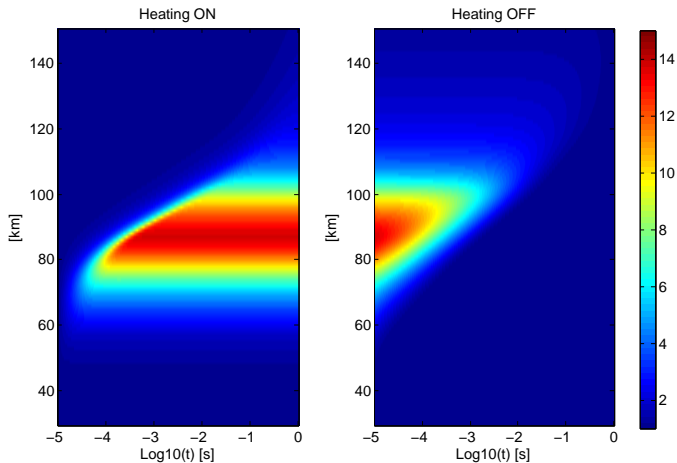
## Example result: 1s on/off heating, $T_e/T_i$

ERP=600 MW,  $f = 5.423$  MHz, O-mode



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# Incoherent scatter spectrum

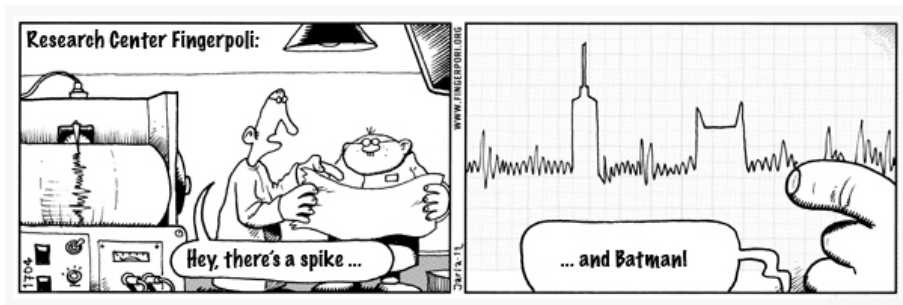


Figure : Fingerpoli, HS, 7 September 2012

# Incoherent scatter spectrum

The spectral density of the incoherent scattering is

$$\sigma(\omega_0 + \omega)d\omega = \frac{N_e r_e^2 d\omega}{\pi} \frac{\left( |y_e|^2 \frac{\sum_j n_j \Re(y_j)}{\omega - \mathbf{k} \cdot \mathbf{v}_{dj}} \left| \sum_j \mu_j y_j + i \lambda_D^2 k^2 \right|^2 \frac{\Re(y_e)}{\omega - \mathbf{k} \cdot \mathbf{v}_{de}} \right)}{\left( \left| y_e + \sum_j \mu_j y_j + i \lambda_D^2 k^2 \right|^2 \right)}.$$

Here

- $n_j = N_j/N_e$  and  $\mu_j = n_j T_e/T_j$  (densities and temperatures),
- $\lambda_D = (\epsilon_0 k_B T_e / N_e e^2)^{1/2}$  (Debye length)
- $k = 2\pi/\lambda$  (wave number).
- $y_j$  (admittance function ... the next slide)

## Incoherent scatter spectrum: Admittance function $y_j$

The admittance functions for the species  $j$  are

$$y_j = \frac{i + (\theta_j - i\psi G_j)}{1 - \psi G_j}.$$

Here the Gordeyev integral (asymptotic expansion) can be written as

$$G_j(\theta_j - i\psi_j, \phi_j, \alpha) = \int_0^\infty e^{-i(\theta - i\psi)t' - \phi^{-2} \sin^2 0.5\phi t' - 0.25t'^2 \cos^2 \alpha} dt',$$

where  $\alpha$  is the angle to the  $\mathbf{B}$  and ...

$$\theta_j = \omega \zeta_j, \phi_j = \frac{eB}{m_j c} \zeta_j, \psi_j = \nu_j \zeta_j, t' = t / \zeta_j, \zeta_j = \frac{1}{k} (m_j / 2k_B T_j)^{1/2}.$$

# Incoherent scatter spectrum: Inputs

What is needed for calculating the IS spectrum?

- Radio wave parameters:  $\omega$ ,  $\mathbf{k}$
- Plasma composition, temperatures, ion masses, coll. frequencies and drift velocities:  $N_j$ ,  $T_j$ ,  $m_j$ ,  $\nu_j$  and  $\mathbf{v}_j$
- Magnetic field  $\mathbf{B}$

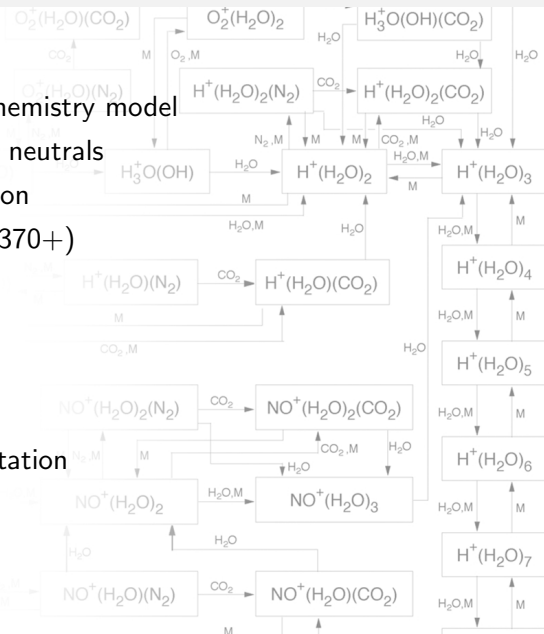
# Sodankylä Ion (and neutral) Chemistry model (SIC)

## Detailed 1-D time dependend chemistry model

- 63 ions (27 negative) & 13 neutrals
- 20-150 km in 1 km resolution
- several hundred reactions (370+)
- vertical transport

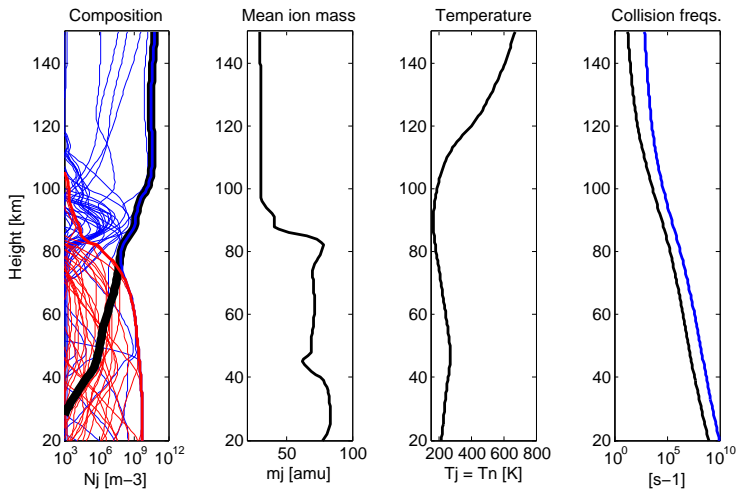
## Input

- MSIS
- solar EM flux
- proton and electron precipitation
- cosmic rays

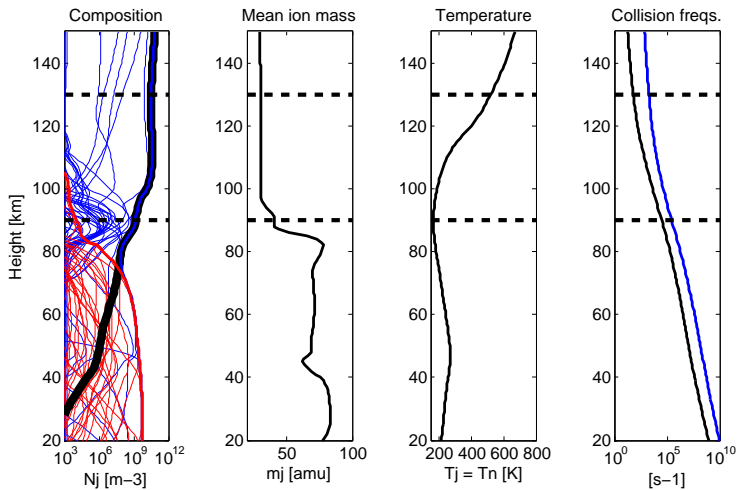




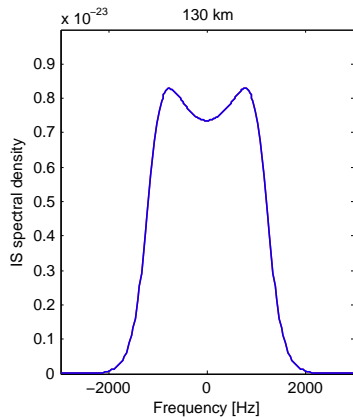
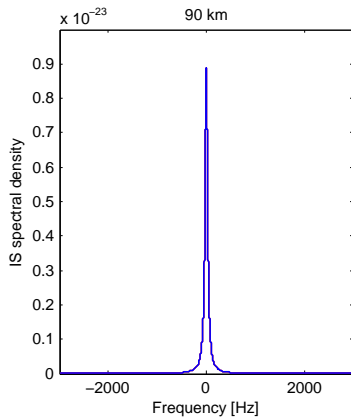
# Input profiles



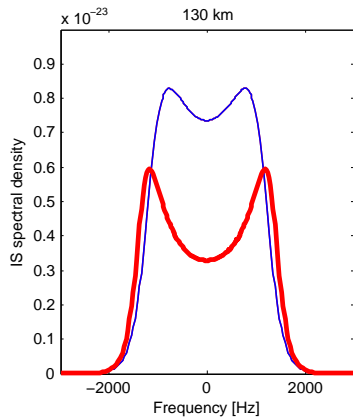
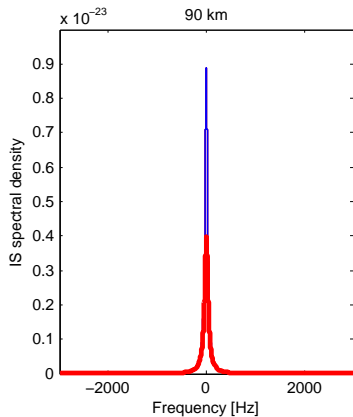
# Input profiles



# Incoherent scatter ion line: 90 and 130 km

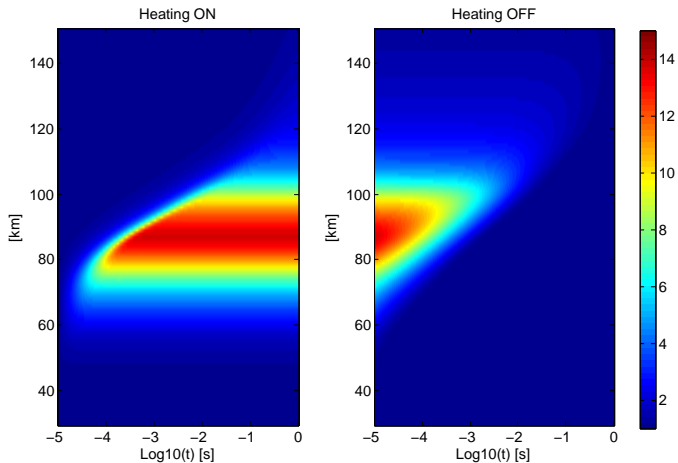


# Incoherent scatter ion line: 90 and 130 km, $T_e = 2T_i$



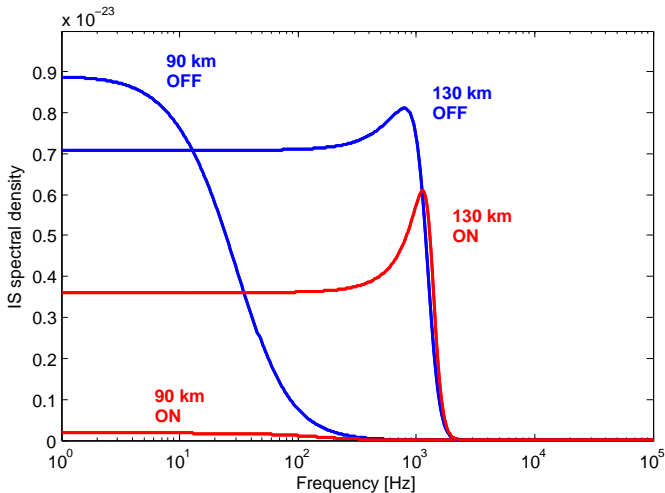
## Example result: 1s on/off heating, $T_e/T_i$

ERP=600 MW,  $f = 5.423$  MHz, O-mode



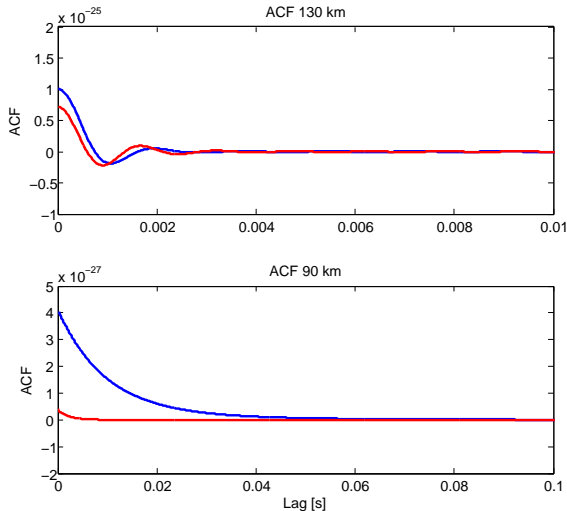
## Example result: 1s on/off heating, the IS spectra

ERP=600 MW,  $f = 5.423$  MHz, O-mode

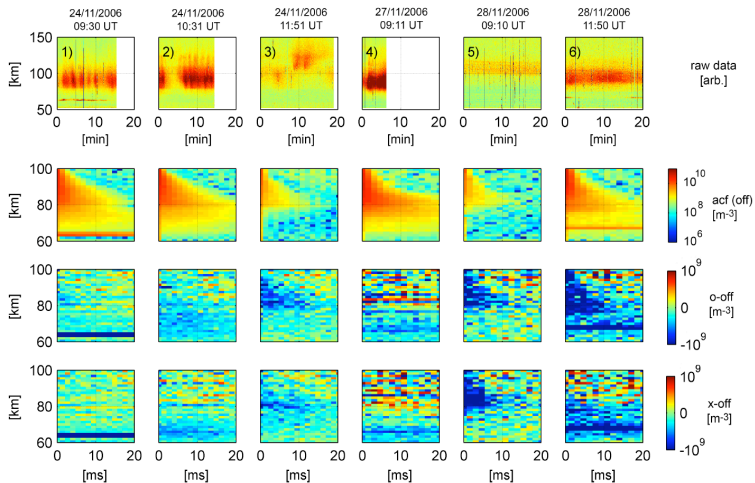


## Example result: 1s on/off heating, the ACFs

ERP=600 MW,  $f = 5.423$  MHz, O-mode

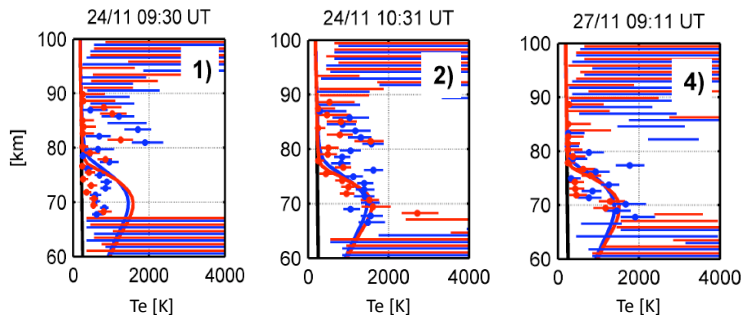


# EISCAT campaign 2006



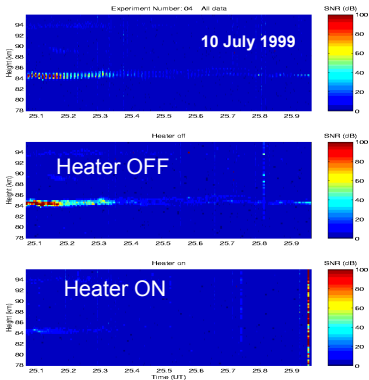


# EISCAT campaign 2006

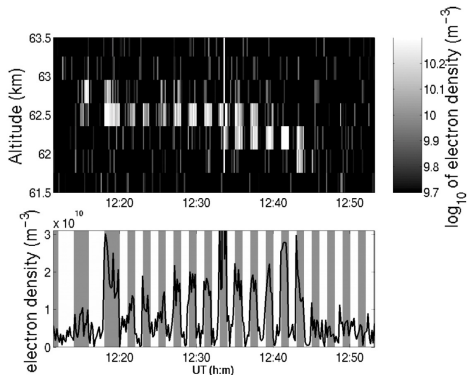


# Coherent scattering: PMSE and PMWE

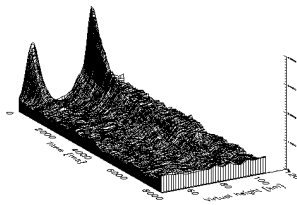
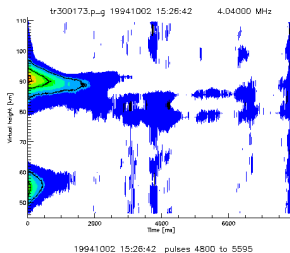
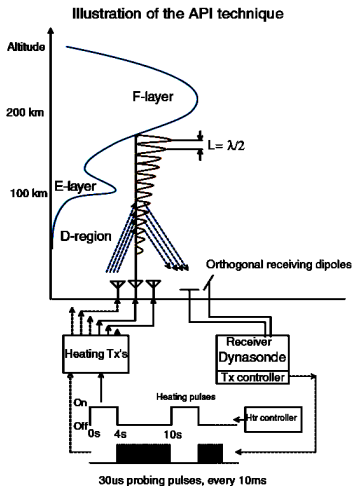
## PMSE at 85 km



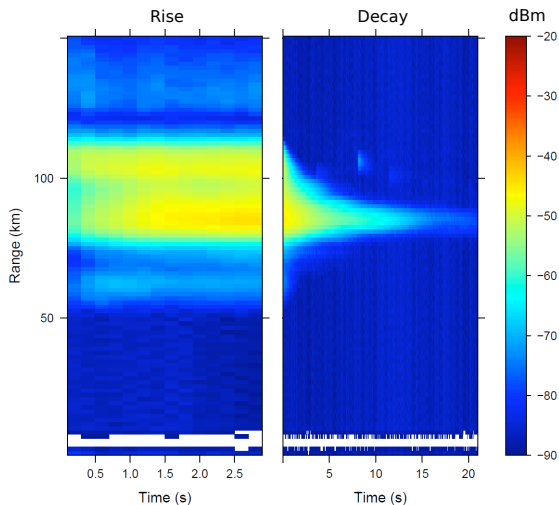
## PMWE at 63 km



# Coherent scattering: Artificial Periodic Irregularities (API)



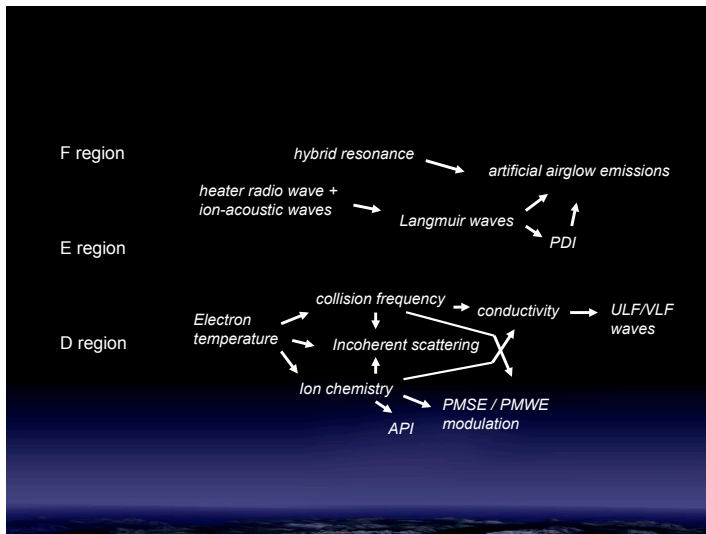
# Coherent scattering: Artificial Periodic Irregularities (API)



# Coherent scattering: summary

	API	PMSE/PMWE
<b>Production</b>	<ul style="list-style-type: none"><li>• standing wave</li><li>• negative ion prod.</li><li>• (dust charging?)</li></ul>	<ul style="list-style-type: none"><li>• turbulence</li><li>• dust/ice charging</li><li>• (negative ions?)</li></ul>
<b>Loss</b>	<ul style="list-style-type: none"><li>• detachment</li><li>• (dust de-charging)</li><li>• (diffusion)</li></ul>	<ul style="list-style-type: none"><li>• diffusion</li><li>• dust de-charging</li><li>• (detachment)</li></ul>
<b>Heating</b>	Forms the irregularities in the first place	Makes the echo <i>weaker</i> (+ builds the overshoot)
<b>Lambda</b>	55.3 m	0.32/1.34/5.35 m

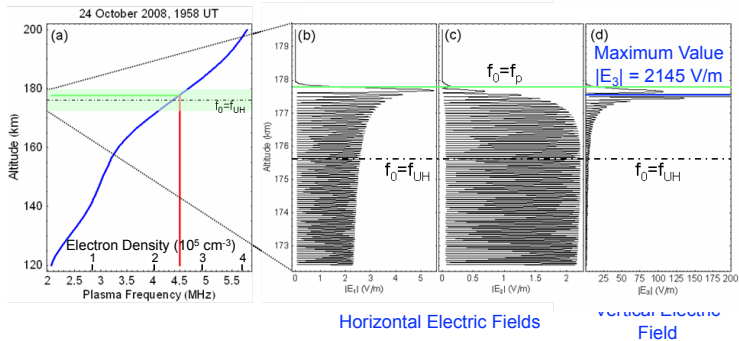
# Some science applications



# Resonance heating



## Full Wave Solution for EM Pump Wave at 4.5 MHz in the Ionosphere Over HAARP

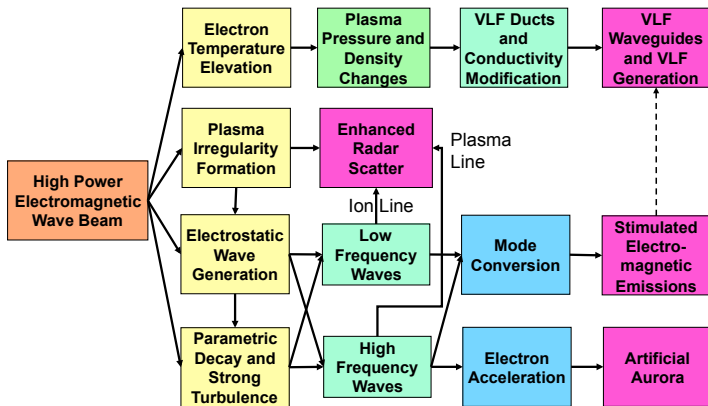


Large Increase in Electric Field Just Below Reflection Altitude where EM Wave Frequency = Plasma Frequency

# Resonance heating



## Ionospheric Modification with High Power Radio Waves





# Resonance heating: artificial airglow

## EISCAT Enhanced Airglow, Bjorn Gustovson, IRFU

